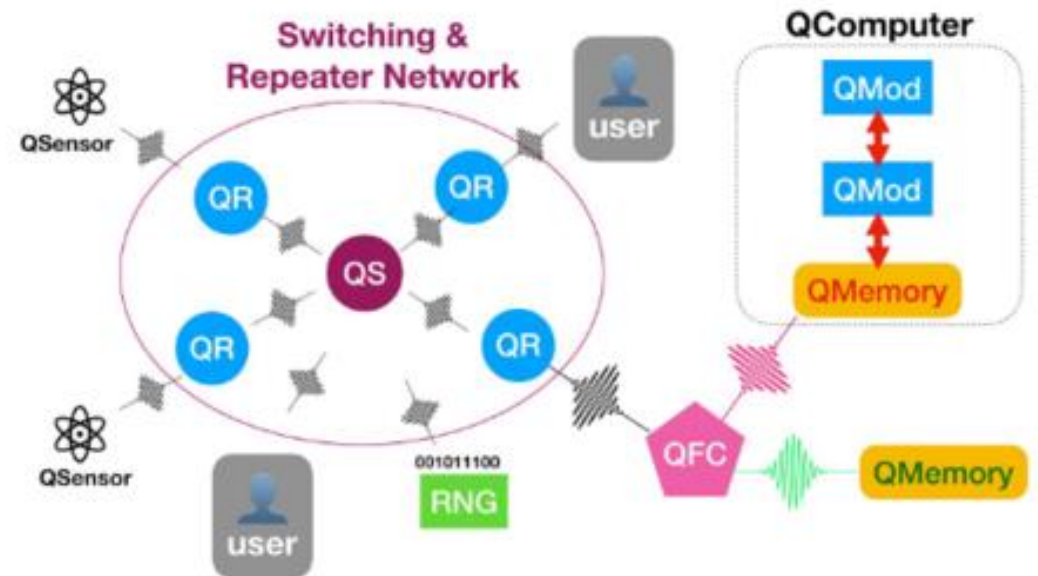


บทที่ 6 AN INTRODUCTION TO QUANTUM NETWORKING

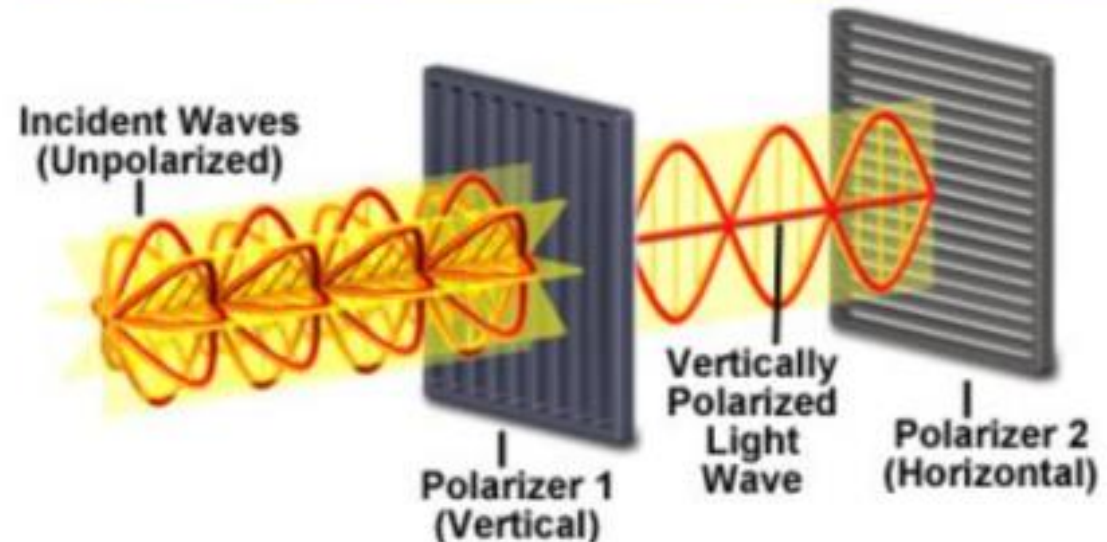
ผู้ช่วยศาสตราจารย์จุฑาภูมิ จันทรมานี

หลักสูตรวิทยาศาสตรบัณฑิต สาขาวิชาวิทยาการคอมพิวเตอร์
คณะวิทยาศาสตร์และเทคโนโลยี มหาวิทยาลัยสวนดุสิต



Photonic Qubits

- Photons can represent Qubits, as well as electrons
- Photons are more conducive to quantum networking than electrons
 - [electrons are more conducive to computing](#)
- The logical states of 0 or 1 are not determined by the spin of photons, but rather by their polarization
 - [Horizontal Polarization](#) $|1\rangle$
 - [Vertical Polarization](#) $|0\rangle$



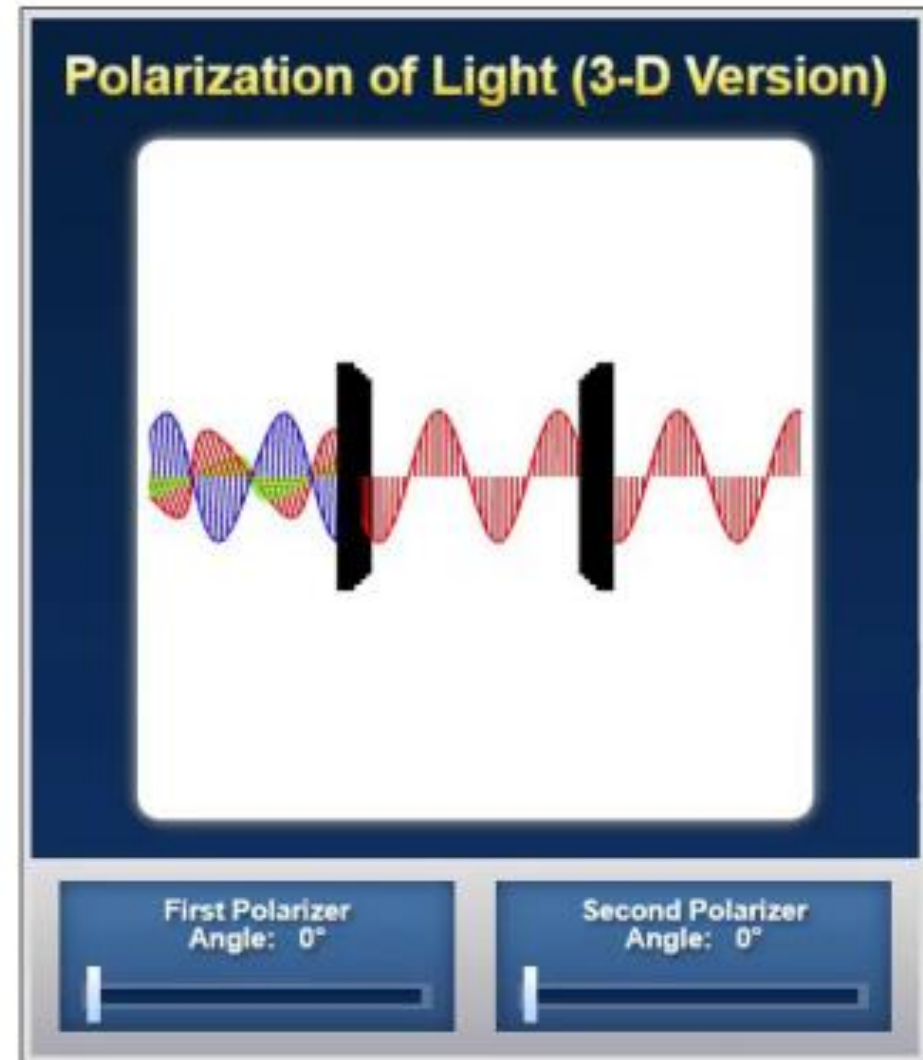
What Happens When Two Waves Intersect?

- When two waves intersect, the resulting displacement of the medium at any location is the **algebraic sum** of the displacements of the individual waves at that same location
- Therefore, another algebraic operation (specifically, a subtraction) can completely reverse the effects of the intersection



Photonic Qubits

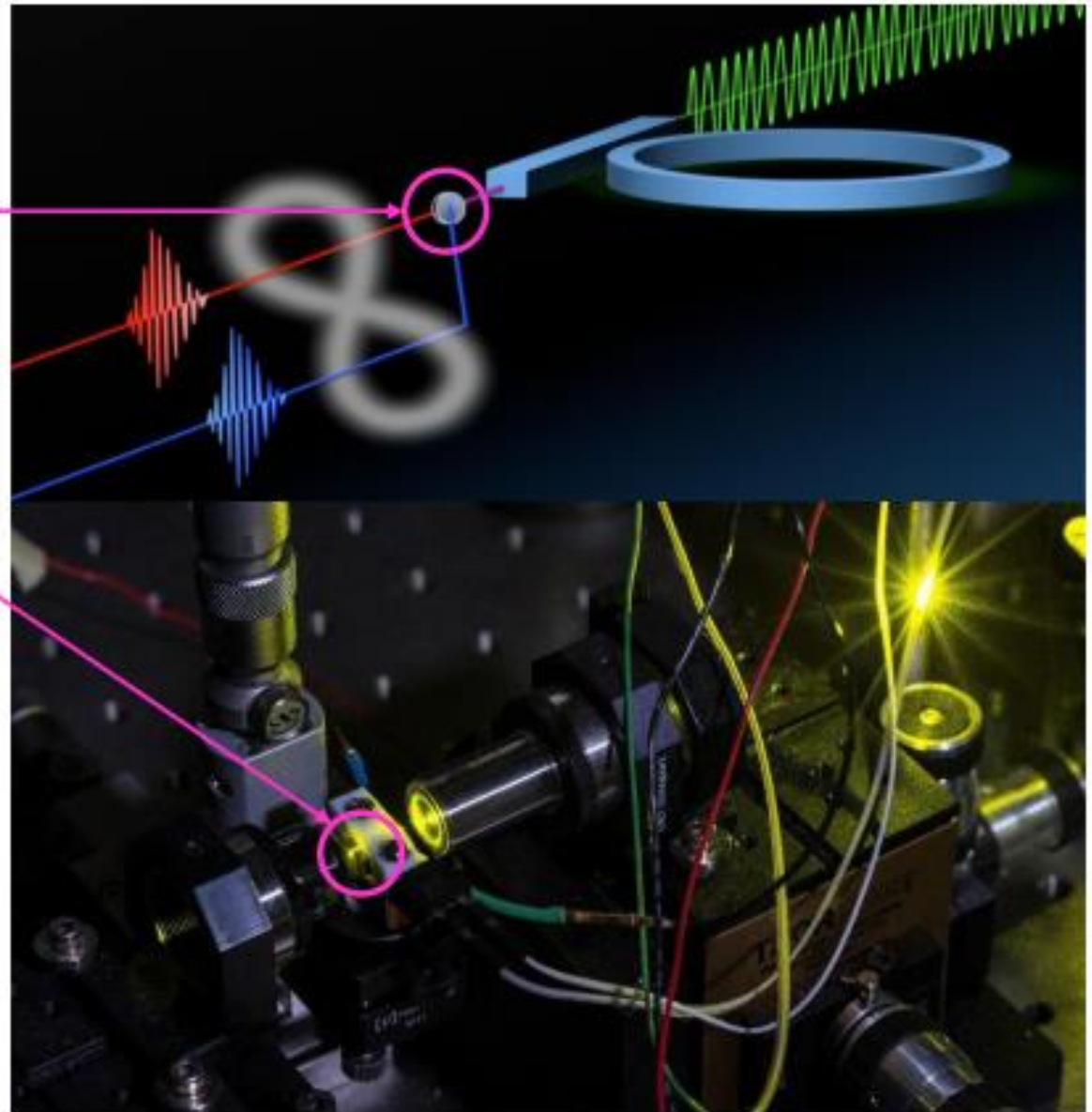
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- Photons are more conducive to quantum networking than electrons (which are more conducive to computing)
- Logical states of 0 or 1 are not determined by spin, but rather by polarization
 - Horizontal Polarization $|1\rangle$
 - Vertical Polarization $|0\rangle$



How Are Photons Entangled?

- The most common approach to generate entangled photons is via **Spontaneous Parametric Down-Conversion (SPDC)** in **nonlinear crystals**
- SPDC is an instant optical process that converts one photon of higher energy into a pair of photons of lower energy

<https://www.nature.com/articles/s41377-021-00537-2>
<https://spectrum.ieee.org/entanglement-on-a-chip>
<https://www.nist.gov/image/non-linear-crystal>



Classical Optical Communication

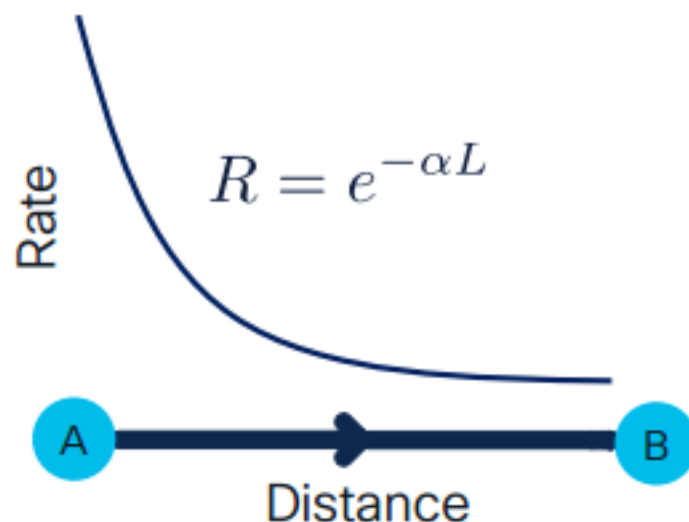


Quantum Communication via Transporting



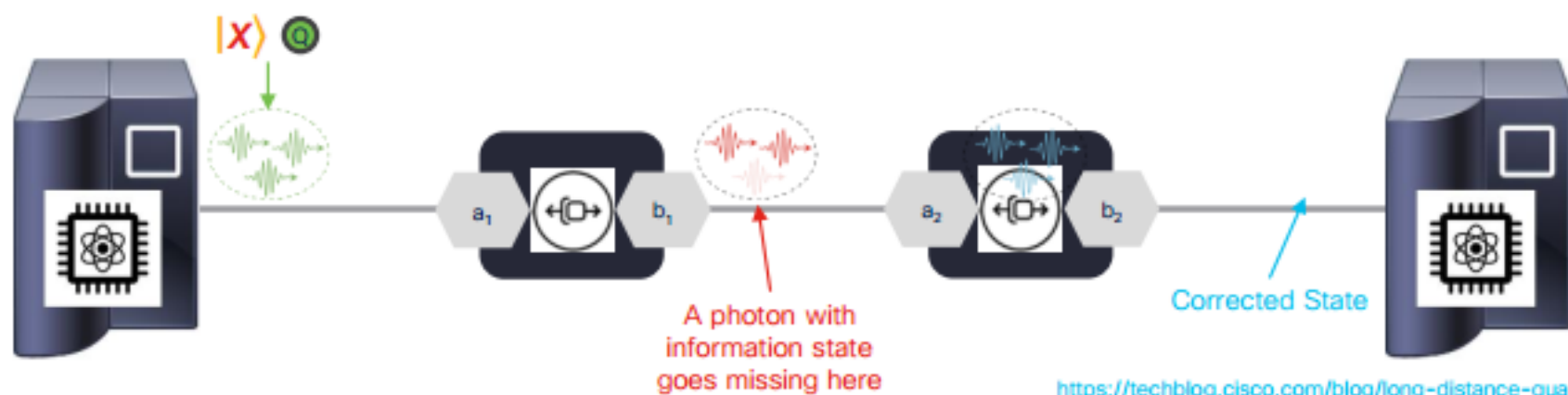
Primary Challenge to Quantum Transport

- Rate decays exponentially with distance
- Can we amplify the signal?
 - No, because of the [No Cloning Theorem](#)



(One-Way) Quantum Repeaters

- Quantum Repeaters leverage Quantum Error Correction, where encoded quantum information is transmitted in the form of multi-photon states
 - Parity information is included in the multi-photon state
- Intermediate repeater stations check the incoming state for errors and prepare a fresh encoded qubit as the output to be sent to the next repeater
- This does NOT violate the [No Cloning Theorem](#), as quantum repeaters perform a multi-qubit measurement that does not disturb the quantum information in the encoded state, but rather, retrieves indirect information about a potential error



<https://techblog.cisco.com/blog/long-distance-quantum-communication>

(Two-Way) Quantum Communication via Teleporting

Initial State



Quantum Communication via Teleporting

Step 1: Entangle a Pair of Photons and Send One to the Receiver



Quantum Communication via Teleporting

Step 2: Perform Another Entanglement Operation at the Sender

Note: This step results in a teleportation of the **combination** of the states of qubits Q and A to qubit B



Quantum Communication via Teleporting

Step 3: Perform a Bell State Measurement at the Sender

Note: The Bell State Measurement simultaneously:

- breaks the three-way entanglement,
- collapses the superpositions of qubits Q and A, and
- produces a result of 1 of 4 Bell States

Note: \otimes is a mathematical notation for a tensor product; that is, a product of two quantum states, $|\psi\rangle$ and $|\phi\rangle$



The Four Bell States:

$|\Phi^+\rangle = (1/\sqrt{2}) (|0\rangle \otimes |0\rangle + |1\rangle \otimes |1\rangle)$ represented by binary 00

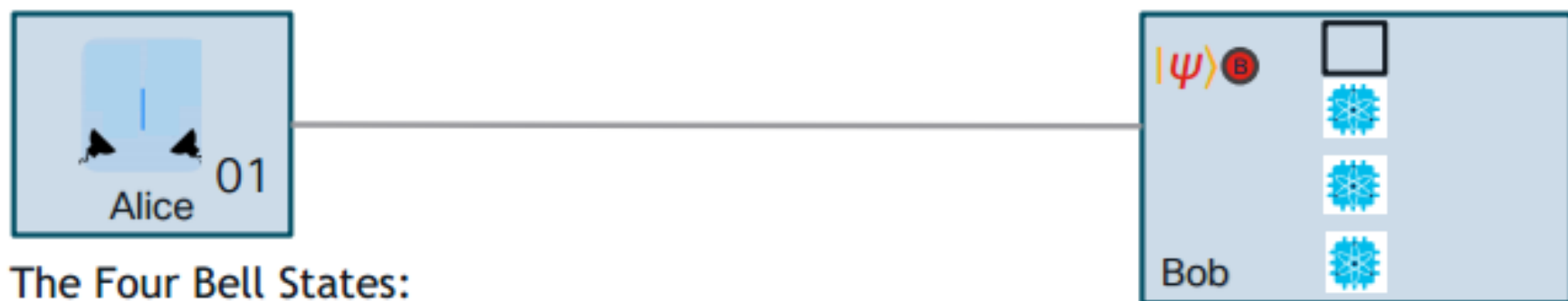
$|\Phi^-\rangle = (1/\sqrt{2}) (|0\rangle \otimes |0\rangle - |1\rangle \otimes |1\rangle)$ represented by binary 01

$|\Psi^+\rangle = (1/\sqrt{2}) (|0\rangle \otimes |1\rangle + |1\rangle \otimes |0\rangle)$ represented by binary 10

$|\Psi^-\rangle = (1/\sqrt{2}) (|0\rangle \otimes |1\rangle - |1\rangle \otimes |0\rangle)$ represented by binary 11

Quantum Communication via Teleporting

Step 4: Send the Bell State Measurement Result over a Classical Channel



The Four Bell States:

$|\phi^+\rangle = (1/\sqrt{2}) (|0\rangle \otimes |0\rangle + |1\rangle \otimes |1\rangle)$ represented by binary 00

$|\phi^-\rangle = (1/\sqrt{2}) (|0\rangle \otimes |0\rangle - |1\rangle \otimes |1\rangle)$ represented by binary 01

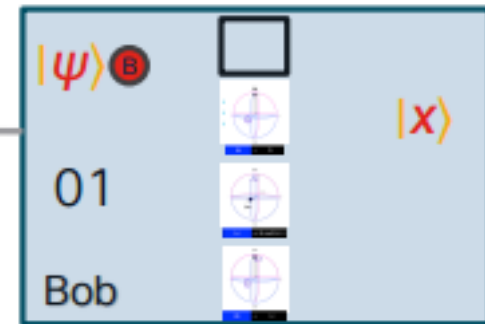
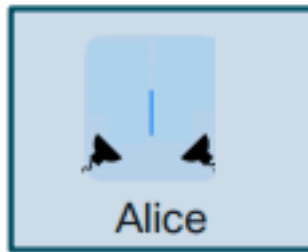
$|\psi^+\rangle = (1/\sqrt{2}) (|0\rangle \otimes |1\rangle + |1\rangle \otimes |0\rangle)$ represented by binary 10

$|\psi^-\rangle = (1/\sqrt{2}) (|0\rangle \otimes |1\rangle - |1\rangle \otimes |0\rangle)$ represented by binary 11

Quantum Communication via Teleporting

Step 5: Perform a Correction Operation on the Received Qubit (if necessary)

Note: $|x\rangle$ represents the original state of the qubit, which has now been received in its corrected form



The Four Bell States:

$|\Phi^+\rangle = (1/\sqrt{2}) (|0\rangle \otimes |0\rangle + |1\rangle \otimes |1\rangle)$ represented by binary 00 → nothing to correct

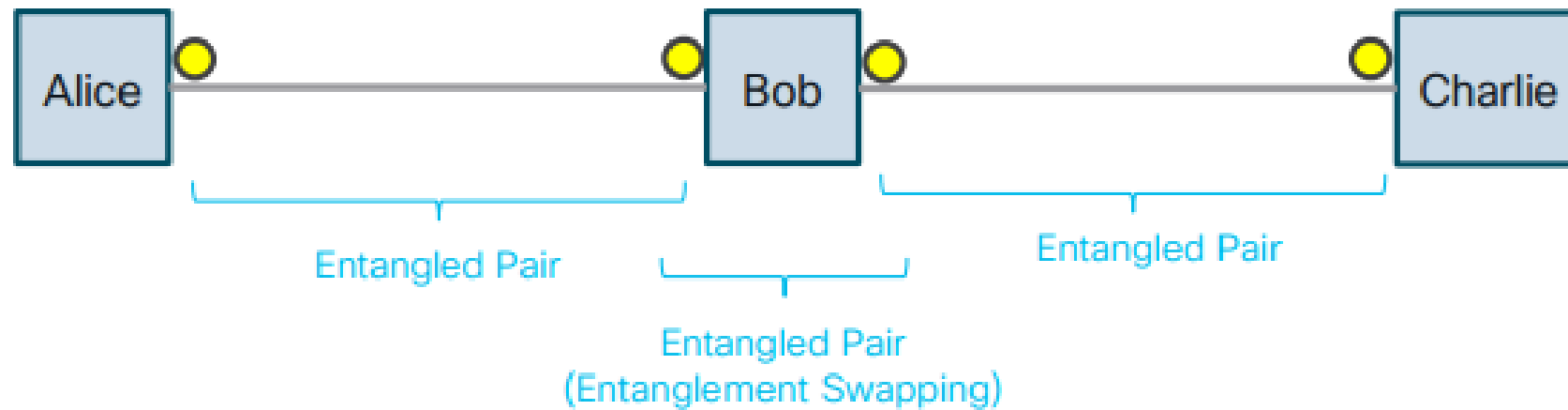
$|\Phi^-\rangle = (1/\sqrt{2}) (|0\rangle \otimes |0\rangle - |1\rangle \otimes |1\rangle)$ represented by binary 01 → correct x (only)

$|\Psi^+\rangle = (1/\sqrt{2}) (|0\rangle \otimes |1\rangle + |1\rangle \otimes |0\rangle)$ represented by binary 10 → correct z (only)

$|\Psi^-\rangle = (1/\sqrt{2}) (|0\rangle \otimes |1\rangle - |1\rangle \otimes |0\rangle)$ represented by binary 11 → correct (x and z)

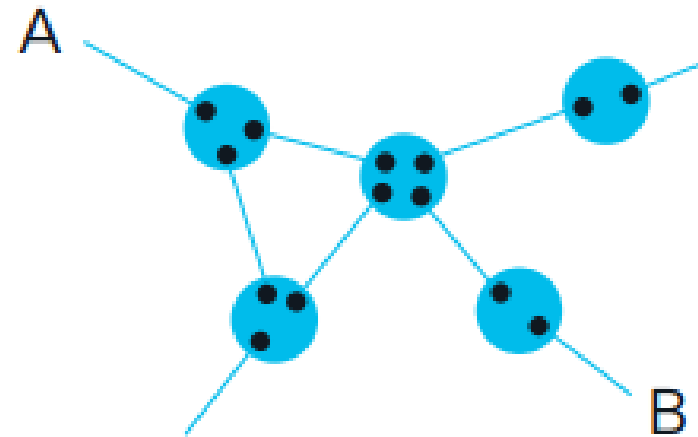
Refer to [Bloch Sphere diagram](#) for x,y and z axis

Extending Quantum Teleporting



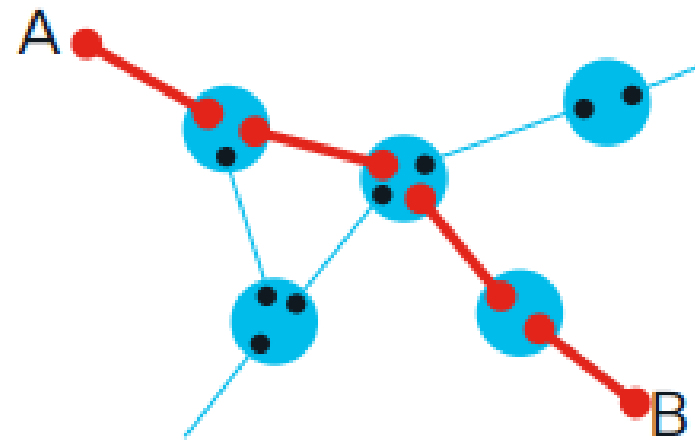
Quantum Routers & Protocols

Two-Way Entanglement Distribution Network Example



Quantum Routers & Protocols

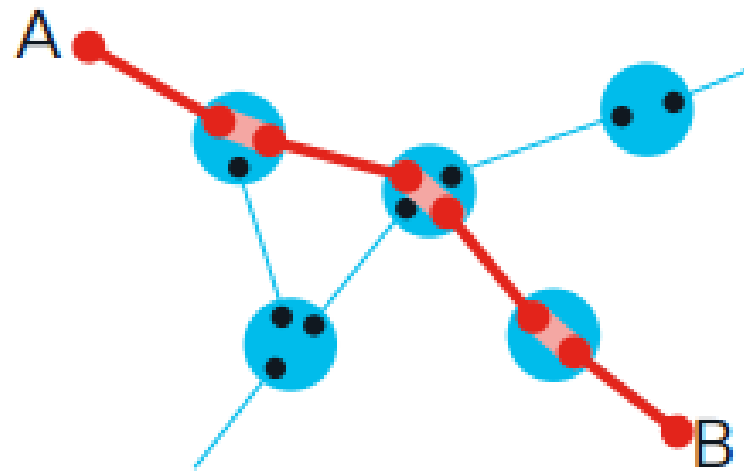
Two-Way Entanglement Distribution Network Example



Elementary link entanglement

Quantum Routers & Protocols

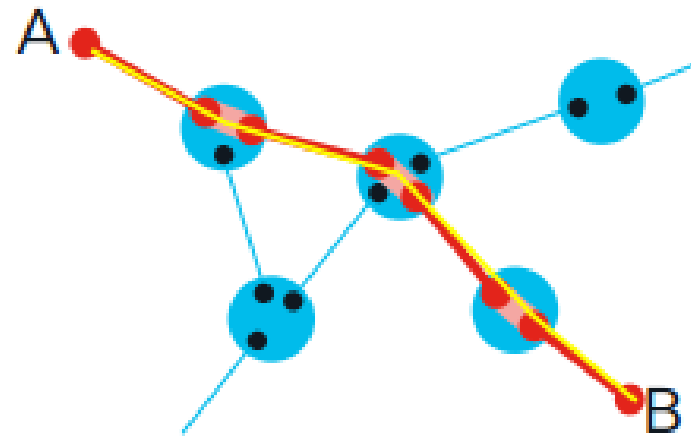
Two-Way Entanglement Distribution Network Example



Elementary swapping

Quantum Routers & Protocols

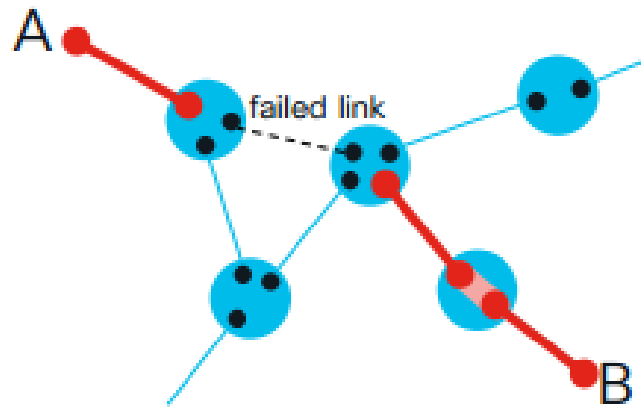
Two-Way Entanglement Distribution Network Example



End-to-end entanglement

Quantum Routers & Protocols

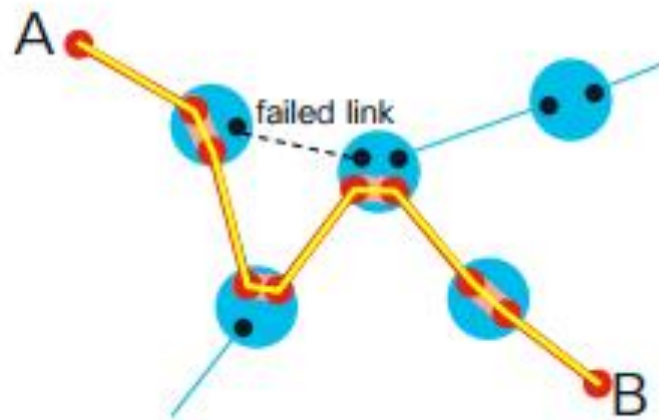
Two-Way Entanglement Distribution Network Example



Network failure event

Quantum Routers & Protocols

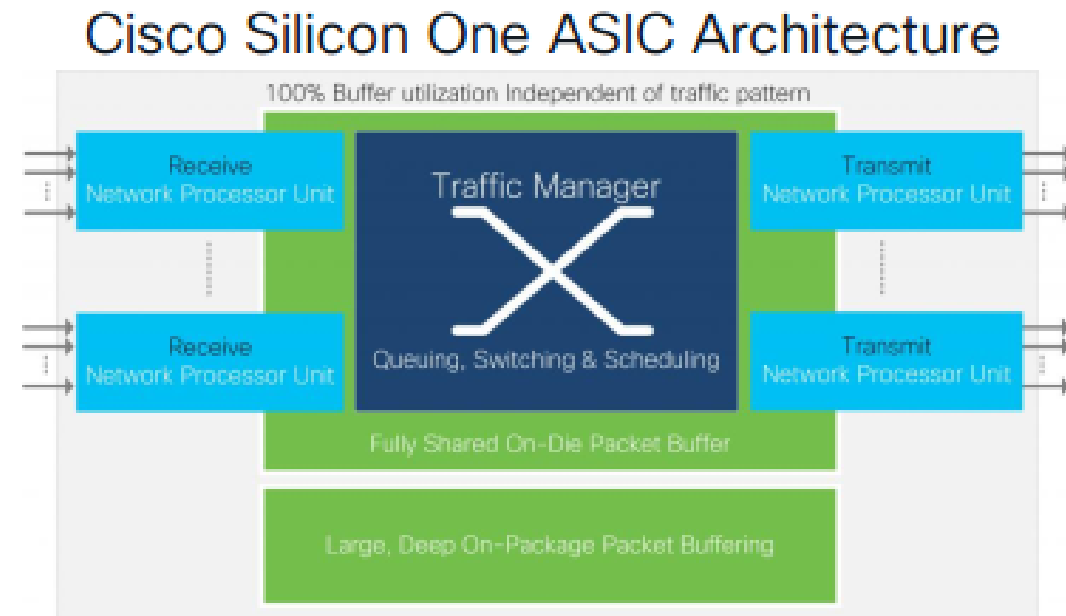
Two-Way Entanglement Distribution Network Example



Reestablishing end-to-end entanglement

The Key Role of Memory in a Network Switch

- A major component of any network switch is memory
- Memory enables:
 - Ingress buffering and queuing
 - Switching
 - Egress buffering and queuing

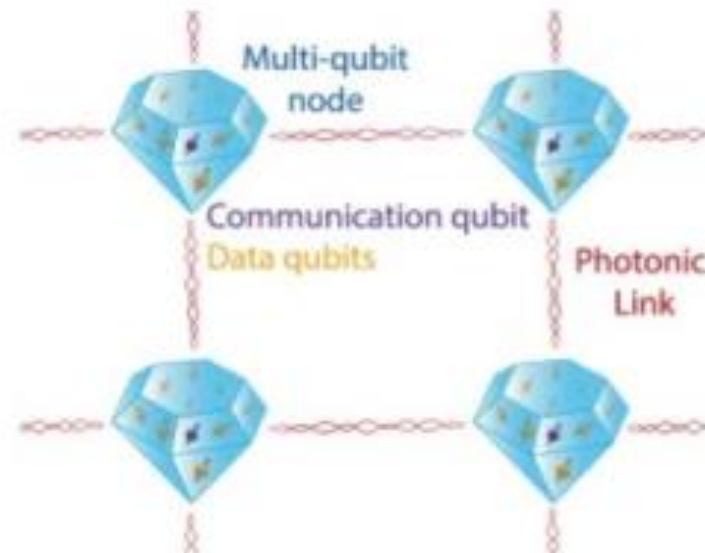


(everything shaded green represents memory)

Note: Cisco Silicon One is **NOT** an ASIC for a quantum switch, but rather is only being used as an example to illustrate how extensive memory is within switching architectures

Quantum Memory Methods and Storage Times

- Optical Quantum Memory
 - milliseconds to seconds.
- Superconducting Qubits
 - microseconds to milliseconds.
- Trapped Ions
 - seconds to minutes
- Note: techniques such as Quantum Error Correction may be employed to extend the effective storage times



An Example of Optical Quantum Memory
Using Engineered Diamonds

<https://www.nature.com/articles/s41534-022-00637-y>

Quantum Networking Challenges by OSI Layer

Application	Cryptography, privacy-preserving computing, enhanced sensing, ...
Transport	End-to-end (logical) quantum information transmission
Network	Routing, Scheduling Quantum circuit switching Error correction, Purification Transporting/Teleporting qubits Photon loss, channel noise, hardware noise
Link	
Physical	

